



Important remarks • This exam measures ILOs no.: a2.1 & b6.3 & c4.1 & c4.2
• No. of pages: 5 - No. of questions: 4

$\epsilon_0 = 10^{-9} / 36\pi$ and $\mu_0 = 4\pi \times 10^{-7}$

Answer all the following questions:

Question # 1 [15 points, 9 points for (a)]:

(a) circle the correct answer for each of the following:

(i) The magnetic field H in a region is: $10\cos(10t+20z) a_y$ A/m. In phasor form this field is:

$10e^{j20z} a_y$ A/m $20e^{j20z} a_y$ A/m $10e^{-j20z} a_y$ A/m $200e^{j20z} a_y$ A/m

(ii) In the following figure the magnetic flux density B is increasing in the direction shown. The induced current i flows in which direction?



Non of these

(iii) An infinitely long wire carries a current of $5\cos(1000t)$ A in the positive z direction. The magnetic field at 0.1 m away from the wire is closest to:

$3 a_\phi$ A/m $5\cos(1000t) a_\phi$ A/m $8\cos(1000t) a_\phi$ A/m $5\sin(1000t) a_\phi$ A/m
 $5 a_z$ mA/m

(iv) The magnetic field H at some point is $10 \cos(10t) a_x$ A/m. The electric field at this point is $20 \cos(10t) a_y$ V/m. The time average power flows in the:

a_x direction $-a_x$ direction a_z direction $-a_z$ direction non of these

(v) An electron is travelling with a velocity of $2a_x$ m/s in a magnetic field with $B = 5 \times 10^{-4} a_x + 2 \times 10^{-4} a_y$ teslas. The force on the electron is:

$5 \times 10^{-20} a_y$ N $6.4 \times 10^{-23} a_x$ N $6.4 \times 10^{-23} a_z$ N $-6.4 \times 10^{-23} a_z$ N

(vi) An electric field in phasor form is $E = (2 a_x + 3j a_y) e^{-j10z}$. The polarization is:

linear left hand circular right hand circular
left hand elliptical right hand elliptical

Please turn over \Rightarrow

(b) A current I flow in the inner conductor of an infinitely long coaxial line and returns via the outer conductor. The radius of the inner conductor a , and the inner and outer radii of the outer conductor are b and c , respectively. Find the magnetic flux density B for all regions and plot B versus r . [6 points]

Please turn over \Rightarrow

Question # 2 (15 points):

(a) Under what conditions will the reflection and transmission coefficients for perpendicular polarization be the same as those for parallel polarization? [3 points]

(b) A uniform plane wave of an angular frequency 3.121×10^9 rad/sec is incident from a very large, perfectly dielectric nonmagnetic medium occupies $x > 0$ space of $\epsilon_r = 2.45$ at an angle $\theta_i = 35^\circ$ to free space with perpendicular polarization. The amplitude of the incident electric field is 50 mv/m. Find [2 points each]:

- the reflection coefficient Γ .
- the transmission coefficient T .
- the Brewster angle θ_b .
- the critical angle θ_c .
- expression for the instantaneous reflected magnetic field, H_r .
- expression for the instantaneous transmitted electric field, E_t .

Please turn over \Rightarrow

Question # 3 (10 points, 4 points for (a) and 6 points for (b)):

(a) The xy-plane serves as the interface between two different media. Medium 1 ($z < 0$) is filled with a material whose $\mu_{r1} = 6$, and medium 2 ($z > 0$) is filled with a material whose $\mu_{r2} = 4$. If the interface carries current of $(1/\mu_0) a_y$ mA/m, and $B_2 = 5a_x + 3a_y + 8a_z$ mWb/m². Find H_1 and H_2 .

(b) A uniform plane wave with $E = E_x a_x$ propagates in a linear isotropic medium ($\mu_r = 1.25$, $\epsilon_r = 4$, $\sigma = 1.8$) in the +z-direction. Assume that the field is sinusoidal with a frequency 100 MHz and has a maximum value of $+10^{-4}$ v/m at $t=0$ and $z=1/8$ m.

- (i) What are the propagation constant, phase constant, and the attenuation constant?
- (ii) What is the wavelength in the medium.
- (iii) Write the instantaneous expression for H at any t and z.
- (iv) Determine the locations where the field E is a positive maximum at $t=10^{-8}$ s.

Please turn over \Rightarrow

Question # 4 (10 points):

For a harmonic uniform plane wave propagating in a simple medium, both E and H vary according with the factor $\exp(-jk.r)$. Show that the four Maxwell's equations for uniform plane wave in a source-free region reduces to the following: [5 points]

$$k \times E = \omega \mu H,$$

$$k \times H = -\omega \epsilon E,$$

$$k \cdot E = 0,$$

$$k \cdot H = 0$$

The current in a long wire is $I = I_0 t$. A small circular loop of 5 cm radius is placed 0.5 m away from the wire in free space. The loop is oriented so that the magnetic flux passing through it is maximized. The voltage induced on this loop is measured at $5.0 \times 10^{-4} \mu_0$ Volts. Find I_0 . State any assumptions that you make.